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The purpose of the research described here was to develop a data structure definition facility (DSDF) and an access control facility suitable for inclusion in high-level programming languages. The research was not intended to include the design of a complete language but instead involved the development of programming language features that aid in the development of languages designed for producing reliable software. The DSDF was to be capable of specifying and implementing a wide variety of views of data. The intentions were to develop a facility capable of defining

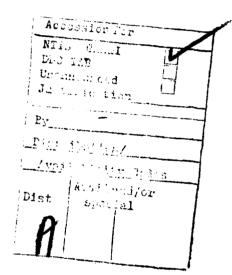
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20. ABSTRACT CONTINUED

real world data objects as well as system-oriented data objects. In addition, the DSDF was to merge the language view of real world and system data objects.



Final Report

U. S. Army Research Office Grant No. DAAG29-78-G-0118

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Data Structure Definition and Access Control Facilities for Languages Designed for the Development of Reliable Software

University of Connecticut, STorrs
September 1, 1978 - August 15, 1979

Billy G. Claybrook

Principal Investigator

Problem Studied

The proposed research was to develop a data structure definition facility (DSDF) and an access control facility suitable for inclusion in high-level programming languages. The research was not intended to include the design of a complete language but instead involved the development of programming language features that aid in the development of languages designed for producing reliable software.

The DSDF was to be capable of specifying and implementing a wide variety of views of data. The intentions were to develop a facility capable of defining real world data objects as well as system-oriented data objects. In addition, the DSDF was to merge the language view of real world and system data objects.

Results of the Research

To meet the objectives of this research, an encapsulation mechanism, the module, was designed for specifying and implementing abstract data types (or data objects) in high-level programming languages. The format of the module is illustrated in Figure 1; it is similar in some respects to other encapsulation mechanisms such as the cluster in CLU [3]. Parameterized types are permitted within the module context and restrictions to them, if any, can be specified. The rights specification is an explicit specification of the rights to objects of the type being defined.

The <u>logical structure</u> (LS) component of a <u>module</u> specification essentially characterizes a data object by defining restrictions to relationships. An LS, by itself, does not specify a data type; instead, it highlights features of a data type and communicates them to the user and to the implementer of the type. To some extent, a logical structure specifies what an object looks like, (independent of any representation). In general, a logical structure component of a

module module name [parameters, if any>] restrictions to parameters rights logical structure 1sname objects attributes relationships invariant assertions semantics of operations constructive nonconstructive representation implementation end module name

Figure 1. Format of a module

module can contain multiple logical structure specifications, each one named (using lsname in Figure 1) and giving a different view of the data type. Normally, however, only one logical structure specification is given per data type.

The semantics of operations can be specified in three ways: (1) by using

the constructive approach described in this paper and in Claybrook, et al. [1], (2) by using Guttag's axioms [2] (only one logical structure specification is meaningful in this case), or (3) by using both the constructive approach and Guttag's axioms. The <u>representation</u> and <u>implementation</u> specifications are self-explanatory.

The Logical Structure

Basically, the logical structure of a data object is characterized by specifying relationships between constituent object types and by defining restrictions to relationships. Each LS specified in the logical structure component of a module is given a name such as GTREE in the genealogy tree data type specified in Figure 2. A logical structure specification can then be referred to by this name. The name(s) of the component object types are given in the objects section. The attributes of each component object are given in the attributes section; they are given in the form of a function from objects to values. The relationship names and the object type(s) involved in a relationship are given in the relationships section. The relationships are binary relationships and are specified in functional form.

module genealogy tree

rights add person, add child

logical structure

lsname GTREE

objects PERSONS

attributes NAME: PERSONS to string

DOB: PERSONS to integer

relationships

CHILDOF:

PERSONS to PERSONS

PARENTOF: PERSONS to PERSONS REDUNDANT
NEXTALPHA: PERSONS to PERSONS REDUNDANT
NEXTOLDEST: PERSONS to PERSONS REDUNDANT

Figure 2. A genealogy tree data type.

invariant assertions Vx,y: PERSONS 1. if x CHILDOF y then DOB(x) > DOB(y) 2. if x ≠ y then NAME(x) ≠ NAME(y) 3. CHILDOF has indegree at most 2 4. CHILDOF is acyclic 5. x CHILDOF y iff y PARENTOF x 6. NEXTALPHA is ordered on NAME and is linear 7. NEXTOLDEST is ordered on DOB and is linear Semantics of operations OCCUR = occurrence <P: collection PERSONS, N: collection NAME, D: collection DOB, CO: CHILDOF, PO: PARENTOF, NO: NEXTOLDEST, NA: NEXTALPHA>

operations wrt GTREE

```
add_person (OCCUR, NEWNAME, SOMEDOB) = if NEWNAME \( \xi \) \( \text{N(n)} \) \( n \in \text{p} \) \\
\text{then ERROR else <P', N', D', CO, PO, NO', NA'> *
\text{where } \text{x: PERSONS and } \text{x \in P}
\( P' = P \cup \( \xi \) \\
\( N' = N \cup \( \xi \xi, NEWNAME > \) \\
\( D' = D \cup \( \xi \xi, SOMEDOB > \) \)
```

end add person

```
add_child (OCCUR, NEWNAME, SOMEDOB, PARENT_NAME1, PARENT_NAME2) =

if NEWNAME \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \)
```

end add_child

end genealogy-tree

Figure 2. (Continued)

*In both the add_person and add_child operations in Figure 2, we indicate that the redundant relations NO and NA are actually affected, even though the operation definitions do not explicitly show this.

The most important ingredient of a logical structure is the invariant assertion. The primary function of the invariant assertion is to specify restrictions to each of the relationships named in the <u>relationships</u> section. In

addition, invariant assertions can also specify relationships between relations (see the genealogy tree data type example in Figure 2 for the relationship between the CHILDOF and PARENTOF relations). The <u>relationships</u> section and the <u>invariant assertions</u> section permit the specifier of a data type to communicate to both the user and the implementer of the data type what he considers to be the type's most important aspects.

The invariant assertions have at least two important uses. First, and perhaps most importantly, they specify what Taylor [4] refers to as the "meaning" of a relationship. For instance, the is-part-of and is-spouse-of relationships are syntactically equivalent but have much different occurrence structures. Secondly, the invariant assertions can be used directly or indirectly to provide a definitive test for valid versus invalid occurrence structures when operations are applied.

The syntax for the assertions is given in Appendix A along with a catalog of properties for relations. Many of these properties are defined using first-order predicate calculus notation. Using names to describe properties makes the invariant assertions easier to read, write and specify.

Semantics of Operations

Previously, we said that the semantics of operations can be specified in three distinct ways: (1) by using the constructive approach described in this paper, (2) by using Guttag's axioms, or (3) by using both the constructive approach and Guttag's axioms.

The operations (constructive approach) are defined in terms of how they affect an occurrence of the data object being specified. An occurrence of a data type is represented as a tuple of elements such as OCCUR in Figure 2. In general, the elements in a tuple consist of collections of instances of all object types, collections of all attribute values, and all relations. For

example, in Figure 2, P is a collection of PERSONS, N is a collection of NAME's, D is a collection of DOB's, and CO, PO, NO, and NA are the four relations restricted by the invariant assertions of the LS named GTREE. An operation definition, then, consists of specifying how the operation affects each of the elements in the occurrence tuple. Not all operations make changes to an occurrence, nor do all operations affect all elements in an occurrence tuple. For example, a find-children operation (not specified) for the genealogy tree data type does not affect an occurrence, and the add_person operation shown in Figure 2 does not change the CHILDOF or PARENTOF relations.

Figure 3 illustrates the stack data type, specified using the principal investigator's constructive approach and Guttag's nonconstructive approach. Redundant specification appears to be useful because Guttag's axioms are useful for verifying that an implementation is correct and the constructive specification is useful as an aid to both the user and the implementer of the type. The utility of redundant specification is a topic of future research.

module stack

rights top, pop, push

logical structure

1sname STK

objects NODE

attributes VALUE: NODE to string

relationships ONTOPOF: NODE to NODE

invariant assertions

1. ONTOPOP is linear

semantics of operations

OCCUR = occurrence <N: collection NODE, V: collection VALUE,

O: ONTOPOF>

Figure 3. stack data type specified (partially specified) using both Claybrook's constructive approach and Guttag's nonconstructive approach

```
operations wrt STK
constructive
       emptystack() = \langle \emptyset, \emptyset, \emptyset \rangle
       push (OCCUR, NEWVALUE) = <N', V', O'>
             where for x: NODE and x \ell N and a \epsilon N \Rightarrow (1y \epsilon N) (<y, a > \epsilon 0)
                                 N^* = \overline{N \cup \{x\}}
                                 V' = V \cup \{<x, NEWVALUE>\}
                                 0' = \underline{if} \ OCCUR = emptystack() \underline{then} \ \emptyset
                                         else 0 \cup \{\langle x, a \rangle\}
       end push
       pop (OCCUR) = if OCCUR = emptystack() then ERROR
             else \langle N', V', O' \rangle
where for x: NODE, x \in N and (Za \in N)(\langle a, x \rangle \in O)
                                 N' = N - \{x\}
                                 V' = V - \{ <_X, V(x) > \}
                                 0' = 0 - \{ \langle x, a \rangle \mid \langle x, a \rangle \in 0 \}
       end pop
       top (OCCUR) = if OCCUR = emptystack() then ERROR
             else V(x), where x \in \mathbb{N} and (y \in \mathbb{N}) (\langle y, x \rangle \in \mathbb{O})
       end top
nonconstructive
       declare stk: stack; elm: integer
             pop(NEWSTACK) = NEWSTACK
             pop(push(stk, elm)) = stk
             top(NEWSTACK) = ERROR
             top(push(stk, elm)) = elm
```

Figure 3. (Continued)

Redundant Relations

end stack

A relation is classified as redundant if it can be totally specified in terms of the attributes and non-redundant relations. Intuitively, a redundant relation does not provide any new information; it merely highlights a particular aspect of the logical structure. NEXTALPHA, NEXTOLDEST and PARENTOF relations are redundant in the genealogy tree logical structure (see Figure 2). CHILDOF is not redundant since it provides new information which cannot be obtained from

the attributes. Note that since CHILDOF and PARENTOF are almost interchangeable, one could have chosen CHILDOF as the redundant relation and PARENTOF as the non-redundant relation. Non-redundant relations must be included in each operation definition, whereas redundant relations need not be included in the operation definition. In some cases, the specifier may choose to define how an operation actually affects a relation, even though the relation is redundant. This approach assures the implementer of all changes that an operation makes to all relations, including redundant relations.

Summary of Results

The significant accomplishments of the year's research efforts include:

- the specification of the <u>module</u> encapsulation mechanism as a means for specifying and implementing abstract data types,
- 2) the development of the <u>logical structure</u> component of the <u>module</u>, in particular the invariant assertions, for specifying restrictions to relationships between constituent object types, and
- 3) the development of the notation for specifying the semantics of operations (using the constructive approach to specification).

The combination of these three things provide the basis for a number of further research topics, including verifying the correctness of implementations of abstract data types. *

^{*} This is one of the objectives of the renewal year of this grant.

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 North-Holland, Amsterdam 1975, pp. 73-84.

Appendix A

This appendix specifies the syntax for invariant assertions and presents a catalog of names that are used to expedite and facilitate the specification of invariant assertions.

An assertion is of the form:

<Relation name> <noise words> <property>

ON <object set>

or assertion in first-order predicate calculus augmented by standard set notations involving the named objects, attributes, and relationships.

Notes

<Relation name> is any relation named in the relationships section of the LS.
<noise words> may be added for readability.

The default value is the set of objects on which relation is defined.

In the following catalog, R stands for the relation parameter and A stands for the object set parameter. Embedded parameters are underlined.

noloops (Va:A) (not aRa).

nocycles ($\forall a:A$) ($\forall n:integer$) ($\not ab_1, b_2, ..., b_n:A$)

(aRb₁ and b_1 Rb₂ and ... and b_n Ra and $a\neq b$ and $n\geq 1$).

acyclic R has noloops and R has nocycles.

indegree n (Va:A) (indegree(a)=n).*

outdegree n (Va:A)(outdegree(a)=n).*

indegree at most n (Va:A) (indegree(a)≤n).*

outdegree at most n (Va:A) (outdegree(a)≤n).*

 $\underline{\mathbf{n}}$: $\underline{\mathbf{m}}$ correspondence R has indegree at most n and R has outdegree at most m.

reflexive (Va:A)(aRa)

symmetric (Va:A) (Vb:A) (aRb iff bRa).

anti-symmetric (Va,b:A)(aRb and bRa implies a=b).

transitive (Va,b,c:A) (if aRb and bRc then aRc).

partition R is reflexive, symmetric and transitive.

partially ordered R is reflexive, anti-symmetric and transitive.

totally ordered R is partially ordered and (Va,b:A)(aRb or bRa).

linear R is acyclic with (card{A} \leq 1 or (\exists a \in A) (indegree (a) =

0 and outdegree (a)=1 and (∃b ∈A) (indegree (b)=1 and outdegree (b)=0 and (∀c:A) (if c≠a and c≠b then

indegree (c) = outdegree (c)=1.)

ordered on x R is linear and (Va,b:A) (aRb implies x(a) < x(b)).

tree A=Ø or $(\exists a:A)$ (indegree (a)=0 and $(\forall b:A)$ (if a≠b then indegree (b)=1)) and R is acyclic.

pair $(\exists a,b:A)(A=\{a,b\} \text{ and } R=\{\langle a,b\rangle\}).$

star ($\exists a:A$)(indegree(a)=0 and ($\forall b:A$) (if $a\neq b$ then indegree (b)=1 and outdegree (b)=0).

set of Y $(\forall P)$ (if $P \subseteq A$ and $(\forall x:P)$ ($\forall a:A$) (a $\not = p$ and (aRx or xRa)) then $R \upharpoonright P$ is Y on P).

forest R is a set of tree.

pairs R is a set of pair.

stars R is a set of star.

.*indegree (a) = card{b|aRb} and outdegree (a) = card $\{b|bRa\}$.

Publications

"Logical Structure Specification and Data Type Definition," Proceedings of the ACM 79 Conference, October 1979, pp. 203-211.

Personnel

Billy G. Claybrook, Principal Investigator (12 months)
Donald Criscione, Graduate Research Assistant (11 months)
Craig Cleaveland, Consultant (1 month)